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Class 09. Sub-.Maths

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8. In right triangle ABC, right angled at C, M is the mid-point of hypotenuse AB. C is joined to M and produced to a point D such that DM = CM. Point D is joined to point B (see Fig. 7.23). Show that:

- (i) $\triangle AMC \cong \triangle BMD$
- (ii) $\angle DBC$ is a right angle.
- (iii) $\triangle DBC \cong \triangle ACB$
- (iv) $CM = \frac{1}{2} AB$

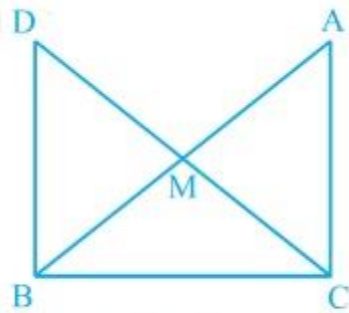


Fig. 7.23

Solution:

It is given that M is the mid-point of the line segment AB, $\angle C = 90^\circ$, and $DM = CM$

(i) Consider the triangles $\triangle AMC$ and $\triangle BMD$:

$AM = BM$ (Since M is the mid-point)

$CM = DM$ (Given in the question)

$\angle CMA = \angle DMB$ (They are vertically opposite angles)

So, by **SAS congruency criterion**, $\triangle AMC \cong \triangle BMD$.

(ii) $\angle ACM = \angle BDM$ (by CPCT)

$\therefore AC \parallel BD$ as alternate interior angles are equal.

Now, $\angle ACB + \angle DBC = 180^\circ$ (Since they are co-interior angles)

$$\Rightarrow 90^\circ + \angle B = 180^\circ$$

$$\therefore \angle DBC = 90^\circ$$

(iii) In $\triangle DBC$ and $\triangle ACB$,

$BC = CB$ (Common side)

$\angle ACB = \angle DBC$ (They are right angles)

$DB = AC$ (by CPCT)

So, $\triangle DBC \cong \triangle ACB$ by **SAS congruency**.

(iv) $DC = AB$ (Since $\triangle DBC \cong \triangle ACB$)

$\Rightarrow DM = CM = AM = BM$ (Since M is the mid-point)

So, $DM + CM = BM + AM$

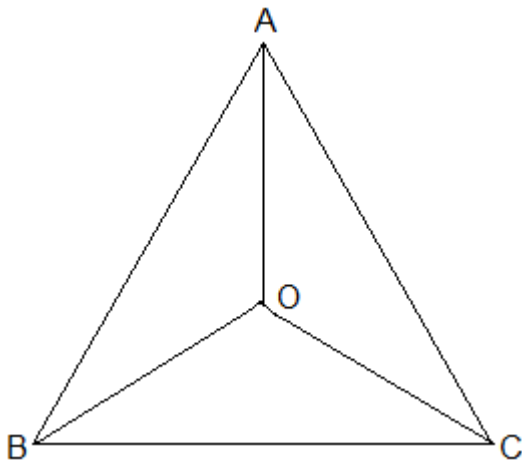
Hence, $CM + CM = AB$

$$\Rightarrow CM = \left(\frac{1}{2}\right) AB$$

Exercise: 7.2 (Page No: 123)

1. In an isosceles triangle ABC , with $AB = AC$, the bisectors of B and C intersect each other at O . Join A to O . Show that:

(i) $OB = OC$ (ii) AO bisects A



Solution:

Given:

$AB = AC$ and

the bisectors of B and C intersect each other at O

(i) Since ABC is an isosceles with $AB = AC$,

$B = C$

$\frac{1}{2} B = \frac{1}{2} C$

$\Rightarrow OBC = OCB$ (Angle bisectors)

$\therefore OB = OC$ (Side opposite to the equal angles are equal.)

(ii) In $\triangle AOB$ and $\triangle AOC$,

$AB = AC$ (Given in the question)

$AO = AO$ (Common arm)

$OB = OC$ (As Proved Already)

So, $\triangle AOB \cong \triangle AOC$ by SSS congruence condition.

$\angle BAO = \angle CAO$ (by CPCT)

Thus, AO bisects A .

2. In $\triangle ABC$, AD is the perpendicular bisector of BC (see Fig. 7.30). Show that $\triangle ABC$ is an isosceles triangle in which $AB = AC$.

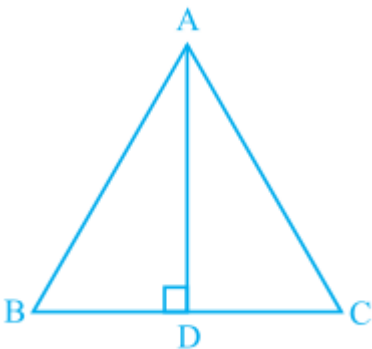


Fig. 7.30

Solution:

It is given that AD is the perpendicular bisector of BC

To prove:

$$AB = AC$$

Proof:

In $\triangle ADB$ and $\triangle ADC$,

$AD = AD$ (It is the Common arm)

$\angle ADB = \angle ADC$

$BD = CD$ (Since AD is the perpendicular bisector)

So, $\triangle ADB \cong \triangle ADC$ by **SAS congruency criterion**.

Thus,

$AB = AC$ (by CPCT)